

# İSTANBUL ANALYSIS SEMINARS

## DILATION THEORY OF INVARIANT KERNELS VALUED IN CONTINUOUSLY ADJOINTABLE OPERATORS OF VH-SPACES

Serdar AY

Bilkent University  
Department of Mathematics

**Abstract:** We consider positive semidefinite kernels that are invariant under an action of a  $*$ -semigroup and valued in the continuous and continuously adjointable operators of VH (Vector Hilbert)-spaces in the sense of Loynes. The main theorem gives two necessary and sufficient boundedness conditions for the existence of an invariant Kolmogorov decomposition of the kernel, or equivalently,  $*$ -representations of the  $*$ -semigroup on a reproducing kernel VH-space. We discuss several cases in which the latter boundedness condition follows automatically. This is a joint work with A. Gheondea.

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Bankalar Caddesi 2, Karaköy 34420, İstanbul