ISTANBUL ANALYSIS SEMINARS

DISTORTION PROPERTIES OF PERTURBED *m*-VALENT JANOWSKI STARLIKE LOG-HARMONIC FUNCTIONS

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Abstract: Let $H(\mathbb{D})$ be the linear space of all analytic functions defined on the open unit disc $\mathbb{D} = \{z | |z| < 1\}$. A sense-preserving log-harmonic mapping is a solution of the non-linear elliptic partial differential equation

$$\overline{f_{\overline{z}}} = w \frac{\overline{f}}{\overline{f}} f_z,$$

where w(z) is the second dilatation of f such that |w(z)| < 1 for all $z \in \mathbb{D}$. It has been shown that if f is a non-vanishing log-harmonic mapping, then f can be expressed as

$$f(z) = h(z)\overline{g(z)},$$

where h(z) and g(z) are analytic in \mathbb{D} . If f vanishes at z = 0 but is not identically zero, then f admits the representation

$$f(z) = z |z|^{2\beta} h(z)\overline{g(z)},$$

where $\operatorname{Re} \beta > -\frac{1}{2}$, and h(z) and g(z) are analytic in D with g(0) = 1 and $h(0) \neq 0$. Let $f = z^m |z|^{2m\beta} h(z)\overline{g(z)}$ be a univalent log-harmonic mapping, where m is a positive integer. We say that f is a Janowski starlike log-harmonic mapping if

$$\operatorname{Re}\left(\frac{zf_z - \overline{z}f_{\overline{z}}}{f}\right) > \frac{1 - A}{1 - B}$$

The class of all Janowski starlike log-harmonic mappings is denoted by $\mathcal{S}_{LH}^*(A, B)$. We also note that if $z^m h(z)$ is an *m*-valent starlike function, then the Janowski starlike log-harmonic mapping $f = z^m |z|^{2m\beta} h(z)\overline{g(z)}$ will be called a perturbed *m*-valent Janowski starlike logharmonic mapping, and the family of such functions will be denoted by $\mathcal{S}_{PLH_m}^*(A, B)$. The aim of the talk is to investigate the distortion properties of perturbed *m*-valent starlike log-harmonic mappings.

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